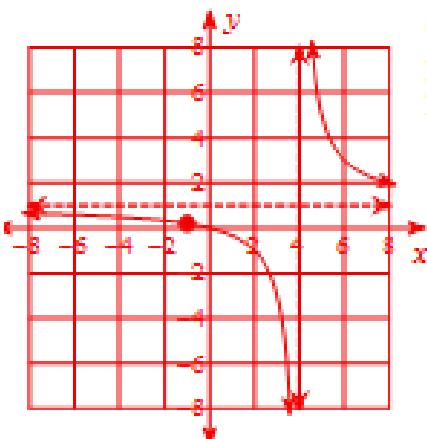


# Thinking Rational

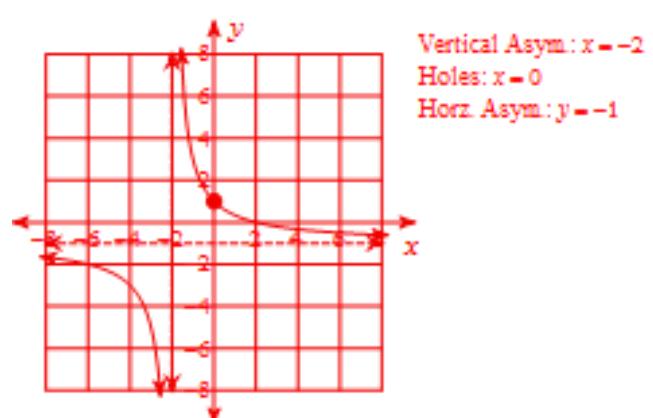
For #'s 1-10, graph the Rational Functions. First find all relevant information needed (intercepts, asymptotes, end behavior, and holes).

1)  $f(x) = \frac{x^2 + x}{x^2 - 3x - 4}$



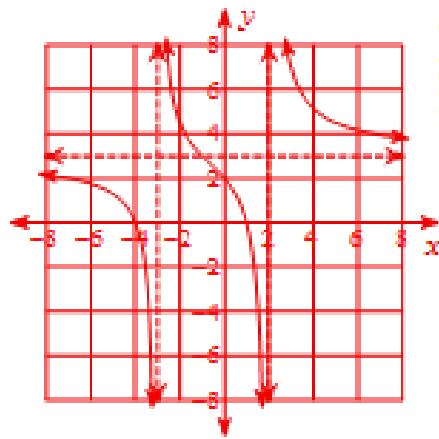
Vertical Asym:  $x = -1$   
Holes:  $x = -4$   
Horz. Asym:  $y = -1$

2)  $f(x) = \frac{-x^2 + 2x}{x^2 + 2x}$



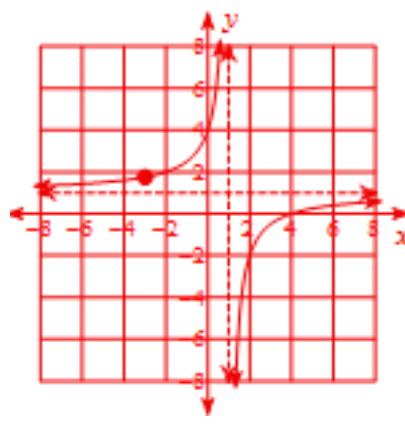
Vertical Asym:  $x = 0$   
Holes:  $x = -2$   
Horz. Asym:  $y = -1$

3)  $f(x) = \frac{3x^2 + 9x - 12}{x^2 + x - 6}$



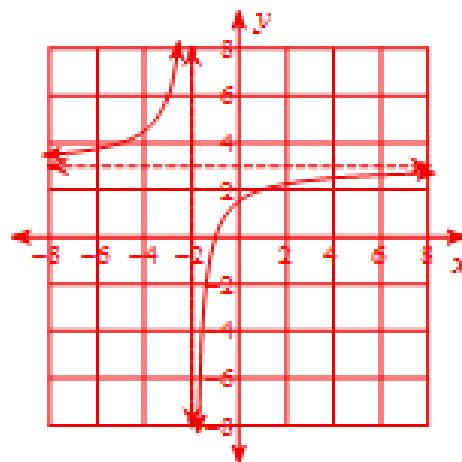
Vertical Asym:  $x = -3, x = 2$   
Holes: None  
Horz. Asym:  $y = 3$

4)  $f(x) = \frac{x^2 - x - 12}{x^2 + 2x - 3}$



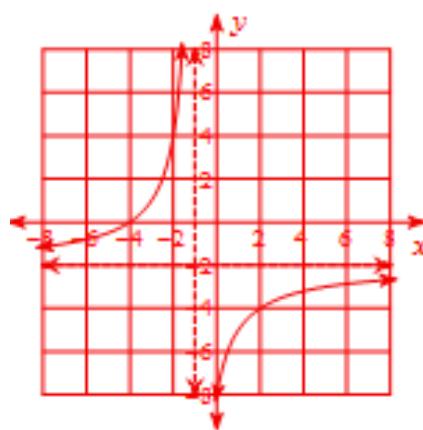
Vertical Asym:  $x = -3$   
Holes:  $x = 1$   
Horz. Asym:  $y = 1$

$$5) \ f(x) = \frac{3x + 3}{x + 2}$$



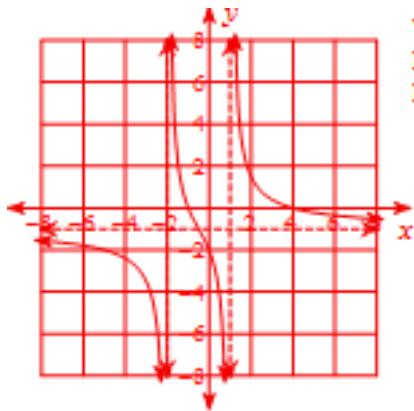
Vertical Asym:  $x = -2$   
Holes: None  
Horz. Asym:  $y = 3$

$$6) \ f(x) = \frac{-2x - 8}{x + 1}$$



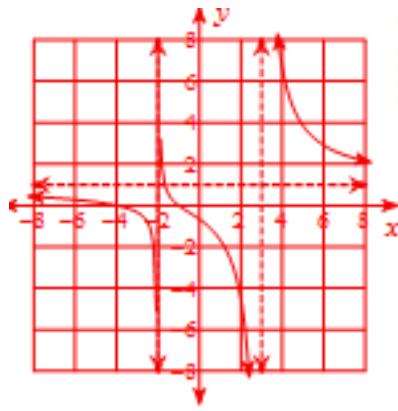
Vertical Asym:  $x = -1$   
Holes: None  
Horz. Asym:  $y = -2$

$$7) \ f(x) = \frac{-x^2 + 3x + 4}{x^2 + x - 2}$$



Vertical Asym:  $x = -1, x = -2$   
Holes: None  
Horz. Asym:  $y = -1$

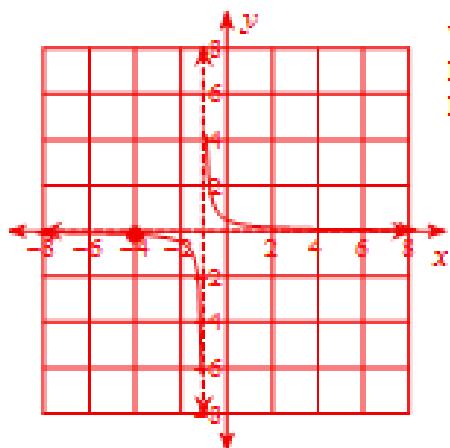
$$8) \ f(x) = \frac{x^2 + 5x + 4}{x^2 - x - 6}$$



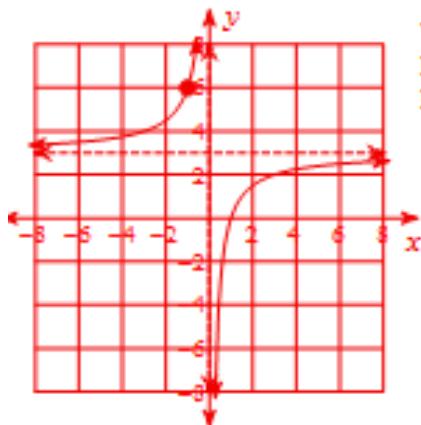
Vertical Asym:  $x = -3, x = 2$   
Holes: None  
Horz. Asym:  $y = 1$

$$9) \quad f(x) = \frac{x+4}{2x^2 + 10x + 8}$$

$$10) \quad f(x) = \frac{3x^2 - 3}{x^2 + x}$$



Vertical Asym:  $x = -4$   
Holes:  $x = -2$   
Horz. Asym:  $y = 0$



Vertical Asym:  $x = 0$   
Holes:  $x = -1$   
Horz. Asym:  $y = 3$

### Bonus:

Find the slant asymptote and sketch a graph (no horizontal asymptote).

$$f(x) = \frac{x^2 - 4x - 5}{x - 3}$$

